

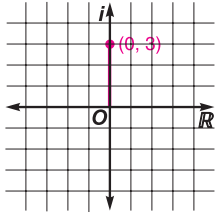
Practice

The Complex Plane and Polar Form of Complex Numbers

Graph each number in the complex plan and find its absolute value.

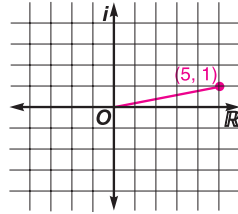
1. $z = 3i$

$|z| = 3$



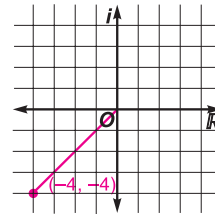
2. $z = 5 + i$

$|z| = \sqrt{26}$



3. $z = -4 - 4i$

$|z| = 4\sqrt{2}$



Express each complex number in polar form.

4. $3 + 4i$

$5(\cos 0.93 + i \sin 0.93)$

5. $-4 + 3i$

$5(\cos 2.5 + i \sin 2.5)$

6. $-1 + i$

$\sqrt{2}(\cos \frac{3\pi}{4} + i \sin \frac{3\pi}{4})$

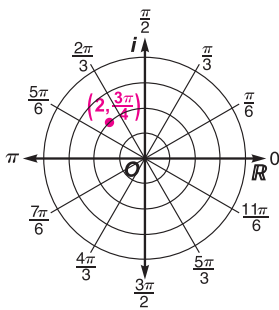
7. $1 - i$

$\sqrt{2}(\cos \frac{7\pi}{4} + i \sin \frac{7\pi}{4})$

Graph each complex number. Then express it in rectangular form.

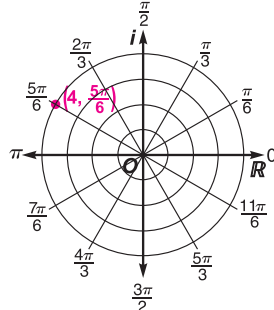
8. $2(\cos \frac{3\pi}{4} + i \sin \frac{3\pi}{4})$

$-\sqrt{2} + \sqrt{2}i$



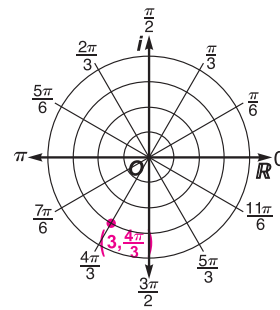
9. $4(\cos \frac{5\pi}{6} + i \sin \frac{5\pi}{6})$

$-2\sqrt{3} + 2i$



10. $3(\cos \frac{4\pi}{3} + i \sin \frac{4\pi}{3})$

$-\frac{3}{2} - \frac{3\sqrt{3}}{2}i$



11. **Vectors** The force on an object is represented by the complex number $8 + 21i$, where the components are measured in pounds. Find the magnitude and direction of the force.

$22.47 \text{ lb}; 69.15^\circ$

En

A Complex Tr

A prospector buried a gold nugget, not telling where the gold was.

1. Start at the oak tree and walk a certain number of paces.
2. Turn 90° to the right and walk a certain stake in the ground.
3. Go back to the oak tree and walk a certain number of paces.
4. Turn 90° to the left and walk a certain stake in the ground.
5. Find the spot halfway between the two stakes. The gold is there.

Years later, an expert found a rusty tin can. Some general area where the rock could be found. The expert located the spring and the trees had sprung up. The expert knew to know which one was the gold through prudent application of the gold. Especially

- The distance between the numbers can be found by the difference.
- Multiplication of a number 90° counter-clockwise rotates it 90° .

The expert drew a map. Let $S(-1 + 0i)$ be the spring location of the oak tree. Let $T(a + bi)$ be the location of the gold.

1. Find the distance between the two points. Express the distance as a complex number $|a + bi|$.
2. Write the complex number in polar form, where the first stake is at the origin.
3. Repeat Exercises 1 and 2 for the rock. Where should the gold be?
4. The gold is halfway between the two locations. Express the location of the gold as a complex number $(0 + 1i)$ axis 1 unit from the origin.